

## 2007 MOTION SAC TEST SOLUTIONS

### Question 1

C

*In John's frame the ball will appear to drop straight down as both he and the ball have the same horizontal velocity.*

### Question 2

(a) Momentum is conserved in all collisions

$P$  (before) =  $p$  (after)

**$V(\text{truck}) = 9.6 \text{ m/s}$**

(b)  $KE$  before =  $2.3 \times 10^5$   
 $KE$  after =  $1.9 \times 10^5$

**Therefore, energy lost =  $3.8 \times 10^4$**

(c) The energy lost in this collision goes mainly into heat and a small amount into sound.

### Question 3

(a)  $F_{\text{net}} = 0$  since travelling at constant velocity.  
 $F(\text{engine}) = F(\text{friction})$   
 $= 750 + 250 = \mathbf{1000N}$

(b)  $F_{\text{net}} = ma$  (caravan)  
 $= T - F_r(\text{caravan})$   
Where  $T$  is the tension in the tow bar

Therefore,  $T = ma + F_r$   
 $= 1000(3) + 250$   
 $= \mathbf{3250N}$

#### Question 4

- (a) **C** (the car at the instant is travelling in the an easterly direction as this is the direction of the tangential velocity)
- (b) **A** The centripetal acceleration acting on the car at the instant shown is towards the centre of the circle (north)
- (c)  $F = mv^2/r$   
 $= 1200 \times 400/60$   
  
 **$= 8.0 \times 10^3 \text{ N}$**
- (d) The friction acting on the car's tyres provides the centripetal force that forces the car to travel in a circle.

#### Question 5

- (a) **C** The projectiles follow parabolic paths

(b)

$$s = ut + 1/2 at^2$$

$$\mathbf{t = 2.5\text{sec}}$$

c) distance = vel x time

$$= 15 \times 2.5$$

$$\mathbf{= 37.5\text{m}}$$

(d)

$$u_v^2 = u_v^2 + 2as \text{ in vertical direction}$$

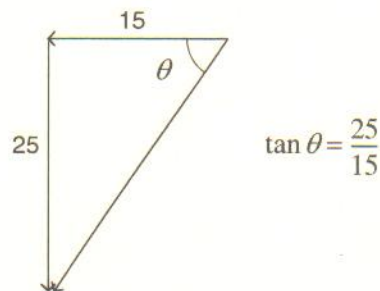
$$\therefore u_v^2 = 0^2 + 2(10)(30)$$

$$u_v = 25 \text{ m s}^{-1}$$

$$v_H = 15 \text{ m s}^{-1}$$

$$\therefore v = \sqrt{V_v^2 + V_H^2}$$

$$= 29 \text{ m s}^{-1} \text{ at } 59^\circ \text{ from horizontal}$$



### Question 6

(a)

$$\begin{aligned} F &= \frac{GmM}{R^2} \\ &= \frac{(6.67 \times 10^{-11})(7.4 \times 10^{22})(6.0 \times 10^{24})}{(3.8 \times 10^8)^2} \\ &= 2.1 \times 10^{20} \text{ N} \end{aligned}$$

(b)

$$\begin{aligned} F &= \frac{GmM}{R^2} = \frac{m4\pi^2 R}{T^2} \\ \therefore T &= \sqrt{\frac{4\pi^2 R^3}{GM}} \\ &= \sqrt{\frac{4\pi^2 (3.8 \times 10^8)^3}{(6.67 \times 10^{-11})(6.0 \times 10^{24})}} \\ &= 2.3 \times 10^6 \text{ s} \end{aligned}$$

(c)

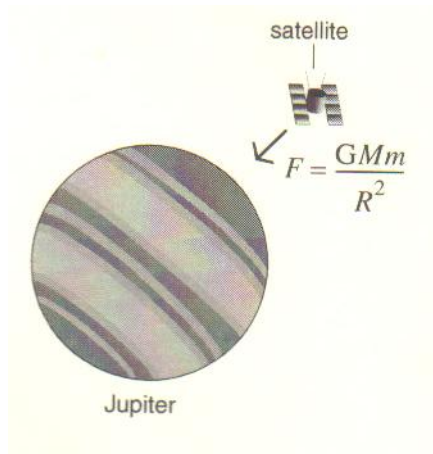
$$\begin{aligned} v &= \frac{2\pi R}{T} \\ &= \frac{2\pi(3.8 \times 10^8)}{(2.3 \times 10^6)} \\ &= 1038 \text{ m s}^{-1} \end{aligned}$$

### Question 7

(a)

$$\begin{aligned} g &= \frac{GM}{R^2} \\ &= \frac{(6.67 \times 10^{-11})(1.9 \times 10^{27})}{(7.22 \times 10^7)^2} \\ &= 24.3 \text{ m s}^{-2} \end{aligned}$$

(b)



### Question 8

(a)

$$9.8 \text{ m s}^{-2}$$

*Accept an answer in the range of 9.7 to 9.9 m s<sup>-2</sup>.*

(b)

$$\text{radius of orbit} = 6400 + 600$$

$$= 7000 \text{ km}$$

$$\text{From graph, } g = 8.2 \text{ m s}^{-2}.$$

*Accept an answer in the range of 8.1 to 8.3 m s<sup>-2</sup>.*

$$\therefore F = mg$$

$$= (1.2 \times 10^3)(8.2)$$

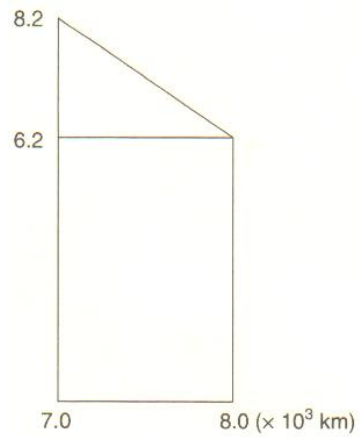
$$= 9.8 \times 10^3 \text{ N}$$

*Accept an answer in the range of  $9.7 \times 10^3$  to  $10 \times 10^3 \text{ N}$ .*

(c)

In this case, energy can be represented by the mass of the space-lab times the area under the force–distance graph between 7000 km and 8000 km from the centre of the Earth. This area is approximately a trapezium as shown.

$$\text{area} = \left( (6.2 \times 1.0 \times 10^6) + \frac{(8.2 - 6.2) \times (1.0 \times 10^6)}{2} \right) m$$



Using  $m = 1200$  kg

$$\text{area} = 8.6 \times 10^9 \text{ J}$$

Accept a range of  $\pm 5\%$ .